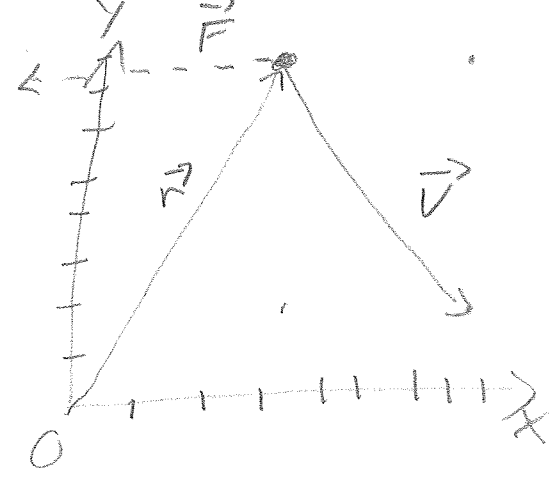


11-33 / $\vec{r} = (3.0\text{ m } \hat{x}, 8\text{ m } \hat{y})$ $m = 3.0\text{ kg}$

$$\vec{v} = (5.0\text{ m/s } \hat{x}, -6.0\text{ m/s } \hat{y})$$

$$\vec{F} = (-7.0\text{ N } \hat{x})$$



Compared to origin,

a) What's angular momentum?

$$\vec{L} = \vec{r} \times m\vec{v}$$

How to do cross products in unit vector notation?

$$\vec{L} = \vec{r} \times m\vec{v} = m (r_x \hat{x} + r_y \hat{y} + r_z \hat{z}) \times (v_x \hat{x} + v_y \hat{y} + v_z \hat{z})$$

(from Eq. 3-30)

$$= m [(r_y v_z - v_y r_z) \hat{x} + (r_z v_x - v_z r_x) \hat{y} + (r_x v_y - v_x r_y) \hat{z}]$$

$$= 3.0\text{ kg} (0 \hat{x} + 0 \hat{y} + (3.0(-6.0) - 5.0(8.0)) \hat{z})$$

$$\vec{L} = -174 \text{ kg m}^2/\text{s } \hat{z}$$

b) $\vec{\tau} = \vec{r} \times \vec{F} = (0 \hat{x} + 0 \hat{y} + (7.0 \cdot 0 - 8.0 \cdot (-7.0))$

$$= +56 \text{ N} \cdot \text{m } \hat{z}$$

c) Just like $\vec{F} = m\vec{a} = \frac{d\vec{p}}{dt}$ in linear motion,

for rotational motion $\vec{\tau} = \frac{d\vec{L}}{dt}$,

and we just found $\vec{\tau}$ in b, so

$$\frac{d\vec{L}}{dt} = \vec{\tau} = 56 \text{ kg m}^2/\text{s}^2 \hat{z}$$